

* Fluid Pressure and Surface tension :-

Ques- What do you mean by fluid pressure
define the cause of fluid pressure.

The force acting normally on unit area of a surface due to fluid is called the fluid pressure.

If the uniform force "F" acts normally on the area "A" of the surface then, pressure "P" on the surface is

$$P = \frac{F}{A}$$

The S.I unit of pressure is N/m^2

or

Pascal.

C.G.S unit is $dyne/cm^2$

And

Dimensional formula is $[ML^{-1}T^{-2}]$

1) Cause of fluid pressure

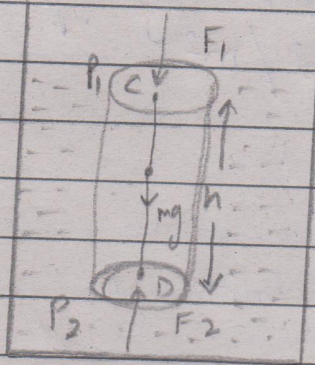
According to the kinetic theory of gases a fluid is made of molecules and molecules are in random motion. They move throughout

the volume of fluid — and suffer collision there is with each other and with the walls of container due to collision there is change in the momentum of molecules. the change in momentum transferred per second by these molecules on the surface gives the average force on the surface.

The force considered on unit surface area gives the fluid pressure.

Ques:- Explain the effect of gravity on fluid pressure.

Consider a vessel having a liquid of density ρ in equilibrium of rest. Let C and D two points inside the liquid at a vertical height "h".



Imagine a cylinder of liquid with axis CD, cross-sectional area A and length h.

The Mass of liquid in the imaginary cylinder

$$m = \text{Volume} \times \text{density}$$

$$m = A \cdot h \cdot \rho$$

Let P_1 and P_2 be the pressure of liquid at point C and D respectively. The action of the following vertical forces.

(i) Force $F_1 = P_1 \times A$ acting vertically downwards on the top face of cylinder.

(ii) Force $F_2 = P_2 \times A$ acting vertically upwards on the lower face of cylinder.

(iii) Weight $mg = A \cdot h \cdot \rho g$ of the liquid cylinder acting vertically downwards.

At equilibrium of the rest the net force on the liquid cylinder must be zero hence,

$$F_1 + mg - F_2 = 0$$

$$F_1 + mg = F_2 \Rightarrow P_1 A + Ah \rho g = P_2 A$$

$$Ah \rho g = P_2 A - P_1 A$$

$$Ah \rho g = (P_2 - P_1) A$$

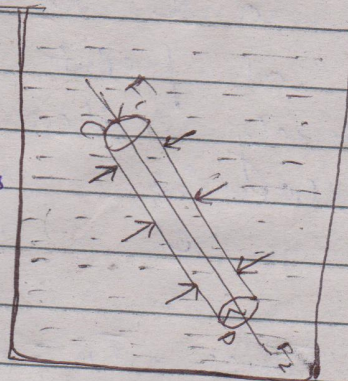
$$\boxed{h \rho g = P_2 - P_1}$$

Ques:- State and prove the Pascal's law:-

→ According to Pascal's law the pressure exerted by fluid is transmitted equally in all directions throughout the liquid.

no pascals law if gravity effect is neglected then pressure at every point of liquid in sq" of sect is same.

In figure, let there be a liquid in a vessel consider a cylinder inside the liquid with its axis CD and its circular surfaces with centre C and D.



Let the force on its surfaces C and D respectively be F_1 and F_2 and area of cross-section be A . Then pressure on the surface C.

$$P_1 = \frac{F_1}{A}$$

$$\text{or } F_1 = P_1 A \quad \text{--- (1)}$$

pressure on the surface D is

$$P_2 = \frac{F_2}{A}$$

$$\text{or } F_2 = P_2 A \quad \text{--- (2)}$$

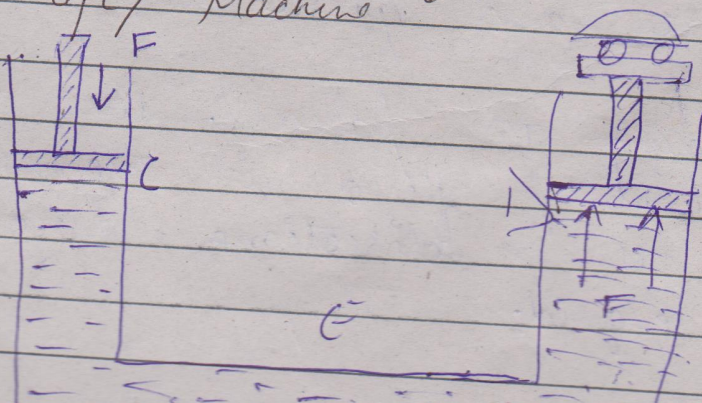
Since, the liquid is in equilibrium hence,

$$F_1 = F_2$$

$$P_1 A = P_2 A$$

$$\boxed{P_1 = P_2}$$

Q. explain the principle of the hydraulic lift/machine.



$$P = \frac{f}{a}$$

$$F = P \cdot b$$

$$F = \frac{f}{a} \cdot b$$

$$F = f \cdot \left(\frac{b}{a}\right) \quad \frac{b}{a} > 1$$

it use. to lift the heavy load
its working is based on Pascal's
law in figure a simple hydraulic
lift is shown in figure
C and D are two cylinders
of different area of cross section
they are connected to each other
with a pipe E. Each cylinder
having a air-tight frictionless
system piston.

Let a, b be the area of
cross-section of the pistons (C and D)
respectively. and $a \ll b$ the
cylinders are filled with an
in-compressible liquid.

Let a downward force f be applied
on the piston of C then the
pressure exerted on the liquid $P = \frac{f}{a}$
acc. to Pascal's law. this press.
is transmitted equally to piston of
cylinder D.

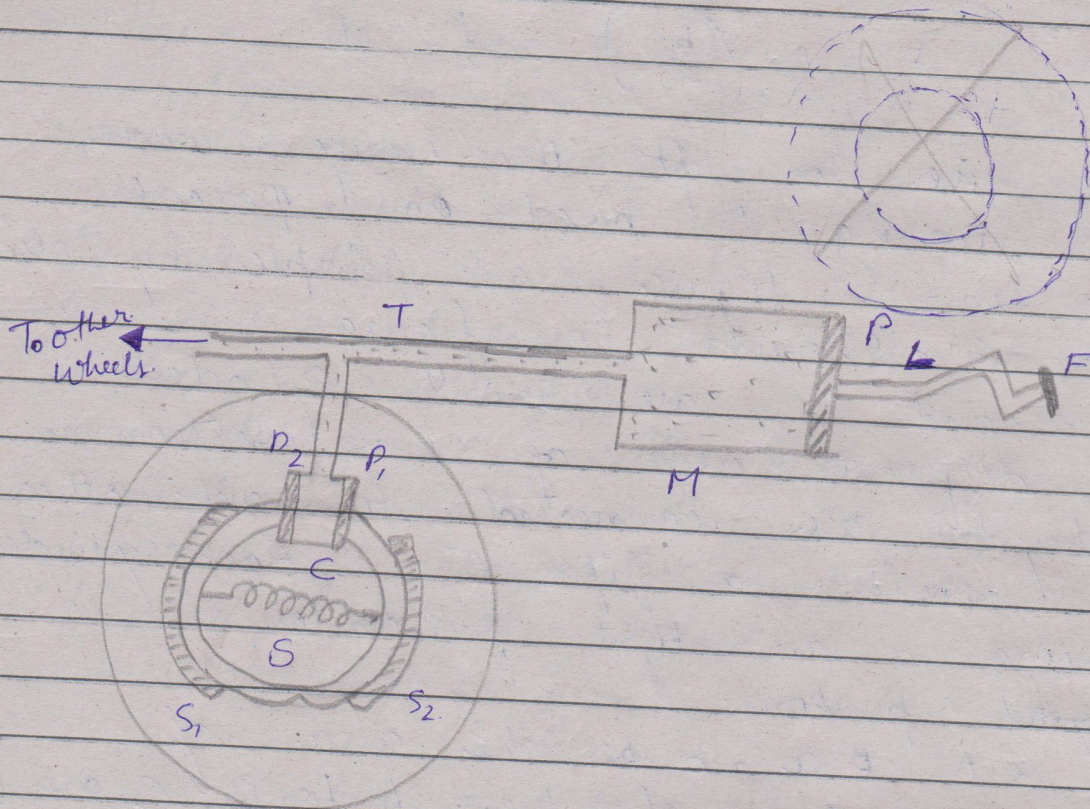
Hence, upward force acting on the
piston of cylinder D.

$$F = P \cdot b$$

$$P = \frac{f}{a}$$

$$F = \frac{f}{a} \cdot b$$

Q Explain construction and working of hydraulic brake.



Construction :-

It consist of a Master Cylinder M filled with brake oil and provided with an airtight frictionless piston P. The piston is connected to break pedal F to lever system. The Master Cylinder is connected to Wheel Cylinder C through a tube T. The wheel cylinder having 2 pistons P₁ and P₂. These pistons are connected to brake shoes S₁ and S₂ respectively. The Spring S hold S₁ and S₂ position.

Working:-

When a break paddle is pressed the lever system operates the piston P of a Master cylinder is ~~pushed~~ pushed inwards. This will increase pressure on liquid at T. Which is transmitted equally P_1 and P_2 of Wheel Cylinder in accordance with the Pascal's Law due to it P_1 and P_2 move outwards they force the break shoe to move away from each wheel which is compressed at the inner rim of wheel hence retards the motion of wheel. When the press on the break paddle is released the break shoe return to their normal position by the action of spring.

Q Write the Laws of Liquid Pressure?

Following are the Laws of liquid pressure.

- 1.) In a stationary liquid pressure is same at all points lying in one horizontal plane.
- 2.) In side a stationary liquid pressure is same at a point in all the directions.
- 3.) Pressure at a point inside the liquid is directly prop- to

Surface.

4.) pressure at a same depth in a different liquid is proportional to density of liquid.

5.) Q What do you mean by atmospheric pressure?

⇒ The weight acting on unit area of ^{earth's} surface due to an air column of unit area of cross-section is called the atmospheric pressure.

The value of atmospheric pressure.

$$P = 1.013 \times 10^5 \text{ N/m}^2$$

$$P = h\rho g$$

$$h = 76 \text{ cm of the Mercury (Hg)} \\ \text{or} \\ 0.76 \text{ m}$$

$$\rho = 13.6 \times 10^3 \text{ kg/m}^3$$

$$g = 9.8 \text{ m/s}^2$$

$$P = 0.76 \times 13.6 \times 10^3 \times 9.8$$

$$P = \underline{1.013 \times 10^5 \text{ N/m}^2}$$

or

$$P = \underline{1.013 \times 10^5 \text{ Pascal}}$$

$$\underline{1 \text{ bar}} = \underline{10^5 \text{ N/m}^2}$$

$$1 \text{ torr} = 1 \text{ mm of Hg}$$

Q. What do you mean by buoyancy and

What are the factors affecting the upthrust force.

⇒ The property of liquid due to which it exerts an upward force on the body emerged inside it, is called buoyancy.

When the body is emerged in a liquid the liquid exerts an upward force on the body this is called upthrust or buoyancy force.

Factor's affecting upthrust:-

The upthrust on the body due to liquid depends on the following 2 factors

1) Vol. of emerged part of the body, -

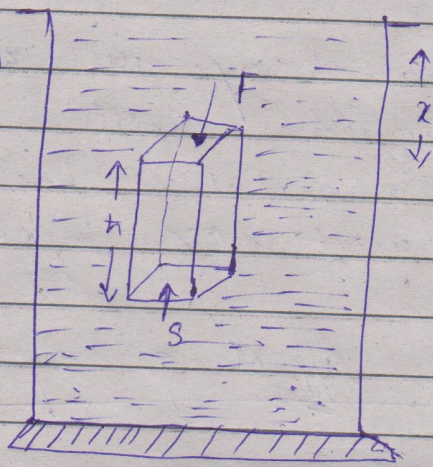
If greater the vol. of emerged part of a body in a liquid, more is the upthrust on it.

2) Density of liquid:- Greater the density of liquid more is the upthrust on the body.

Q. State and prove the Archimedes principle.

According to the Archimedes principle.
 When a body is emerge completely
 or partly in a liquid
 at Rest; it loses some of
 its weight the loss in weight
 of a body in a liquid is
 equal to the weight of the
 liquid displaced by the emerge
 part of the body.

Consider a rectangular
 body of height " h "
 and Mass " M "
 emerged in a liquid
 of Density ρ . Let
 the top and
 bottom faces of
 the body be



parallel to the horizontal base of the
 container. Let " x " be the depth of
 the top face of body below
 the free surface of the liquid hence
 depth of bottom face of the
 body = $x+h$

Let A be the cross-sectional area
 of the top or bottom face of the
 body. Hence,
 Volume of liquid displaced =

$$V = \text{volume of the body}$$

$$V = Ah$$

Mass of liquid displaced

$$m = V\rho$$

$$m = Ah\rho \quad (1)$$

$$P = h\rho g$$

Liquid pressure on the top face of the body.

$$P_1 = x\rho g$$

Vertical downward thrust on the top face of the body

$$F_1 = P_1 A$$

$$F_1 = x\rho g A \quad (2)$$

Liquid pressure on the bottom face of the body.

$$P_2 = (x+h)\rho g$$

Vertical upward thrust on the bottom face of the body

$$F_2 = P_2 A$$

$$F_2 = (x+h)\rho g A \quad (3)$$

from (2) and (3)

$$F_2 > F_1$$

Hence, net upward thrust acting on the body.

$$F = F_2 - F_1$$

$$F = (x+h)\rho g A - x\rho g A$$

$$F = (x+h-x)\rho g A$$

$$F = h\rho g A$$

$$F = \boxed{A h \rho g}$$

$F = \frac{\rho V g}{\rho_{\text{liquid}}}$
upward thrust $F =$ weight of the displaced liquid

Actual weight of the body $(W) = Mg$

Hence; observed weight on the body in liquid. $= W - F$

$$= Mg - mg$$

Thus observed weight of the body emerge in a liquid become less than its ^{of actual} true weight by an amount equal to the weight of the liquid displaced by the body.

Q. What do you mean by Cohesive ~~Force~~ and adhesive force.

The force of attraction b/w the molecule of same substance is called Cohesive force.

The force of attraction b/w the molecules of different substance is called the adhesive force.

Q. What do you mean by Surface Tension. Write the definition of the Surface Tension

⇒ Concept:-

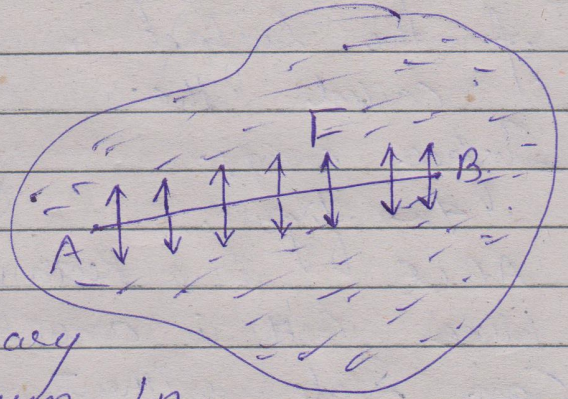
Liquid has a property that its free surface behaves like

Stretched elastic membrane and
 Has a Natural Tendency to contract
 i.e., the free surface of a liquid
 Tends to occupy a Minimum
 Surface area. This property of liquid
 is called the Surface Tension.

Definition

Figure Represents

the free surface
 of a liquid on
 which an imaginary
 line AB is drawn in
 any direction. The surface on either
 side of this line exerts an attractive
 force on the surface on other side.
 This force lies on the plane of the
 surface and is normal to the
 line AB. If the length of line
 AB is l and the total
 force acting on it is F then
 Surface Tension $T = \frac{F}{l}$



if $l = 1$ then $T = F$

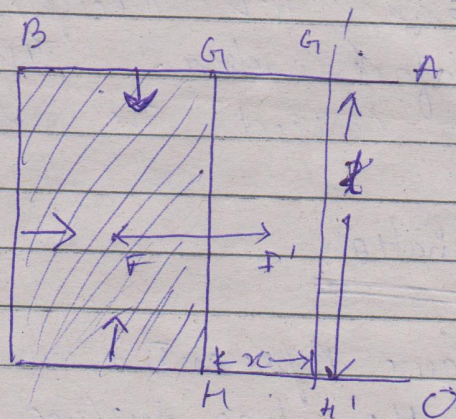
Surface ^{Tension} of liquid is defined as the
 force per unit length in
 the plane of the liquid
 surface acting normally on
 either side of an imaginary
 line drawn in that surface.

Q. What do you mean Surface energy. Derive the expression for Surface energy.

The potential energy store per unit Area of the Surface is called the Surface energy.

In figure,

ABCD is a Rectangular frame of wire. GH is another wire which can slide without friction. A film is formed without emerging it in a Soap Solution. The film has 2 Rectangular Surfaces the upper and Lower Surface.



The force on the wire GH due to Surface Tension is $F =$

$$F = T \cdot 2l \quad \text{--- (1)}$$

When T is the Surface Tension of Liquid. To keep the wire GH at its position a force = F acting outwards is Required on it, if the wire GH is displaced to a distance x by the force F then work done on the wire

$$W = F \cdot x$$

$$W = T \cdot 2l \cdot x$$

$$W = T \cdot \Delta A \quad \text{--- (2)}$$

if $\Delta A = 1$ then;
 $T = W$

Hence, The Surface Tension of a liquid is equal to the work require to increase the Surface Area of liquid film by Unity at the Constant Temperature.

Ques:- Derive the expression for Work Done when a big Drop Divides in small droplets or small drops combine to form a Big Drop.

When a big liquid Drop splits into a No. of small Drop of equal size we have to do some work and the surface energy of some Drops increase. When small liquid Drop each of equal size combine to form a big drop some energy is Released. And then the surface energy is decrease.

Let a big Drop of Radius R splits into n small Drops each of Radius r then;
Vol. of big Drop = $n \times$ vol. of one small Drop.

$$\frac{4}{3} \pi R^3 = n \times \frac{4}{3} \pi r^3$$

$$R^3 = n r^3$$

$$R = n^{1/3} \cdot r \quad \text{--- (1)}$$

$$V = n^{1/3} \cdot r^3$$

$$\text{Surface Area of } 1 \text{ big Drop} = 4\pi R^2$$

$$\begin{aligned}
 \text{Surface Area of } n \text{ Small Drop} &= n \times 4\pi R^2 \\
 &= n \times 4\pi \left(n^{\frac{1}{3}} R\right)^2 \\
 &= n \times 4\pi n^{\frac{2}{3}} R^2 \\
 &= n^{\frac{1}{3}} \cdot 4\pi R^2
 \end{aligned}$$

Increase in Surface Area. =

$$\begin{aligned}
 \Delta A &= n^{\frac{1}{3}} \cdot 4\pi R^2 - 4\pi R^2 \\
 \Delta A &= 4\pi R^2 \left(n^{\frac{1}{3}} - 1\right)
 \end{aligned}$$

$$W = T \cdot \Delta A$$

$$\Rightarrow W = T \cdot 4\pi R^2 \left(n^{\frac{1}{3}} - 1\right)$$

$$W = 4\pi R^2 T \left(n^{\frac{1}{3}} - 1\right)$$

Q. A Needle of Length 5cm is on the Surface of Water the Surface Tension of Water $7.3 \times 10^{-2} \text{ N/m}$ What force is Needed other than the weight of a Needle to Lift the Needle above the Surface of Water.

$$\Rightarrow F = T \cdot 2L$$

$$\Rightarrow F = 7.3 \times 10^{-2} \times 10$$

$$\Rightarrow F = 73 \times 10^{-2}$$